

# *Background subtraction techniques: a review*

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# Agenda

- The problem
- The basic methods
- Running Gaussian average
- Mixture of Gaussians
- Kernel Density Estimators
- Mean-shift based estimation
- Combined estimation and propagation
- Eigenbackgrounds

# The problem

- Main goal: given a frame sequence from a fixed camera, detecting all the foreground objects
- Naive description of the approach: detecting the foreground objects as the difference between the current frame *and an image of the scene's static background*:

$$| frame_i - background_i | > Th$$

- First consequent problem: how to automatically obtain the image of the scene's static background?

# The problem - requirements

The background image is not fixed but must adapt to:

- Illumination changes
  - gradual
  - sudden (such as clouds)
- Motion changes
  - camera oscillations
  - high-frequencies background objects (such as tree branches, sea waves, and similar)
- Changes in the background geometry
  - parked cars, ...

# The basic methods

## Frame difference:

$$|frame_i - frame_{i-1}| > Th$$

- The estimated background is just the previous frame
- It evidently works only in particular conditions of objects' speed and frame rate
- Very sensitive to the threshold  $Th$

# The basic methods (2)

Frame difference: an example

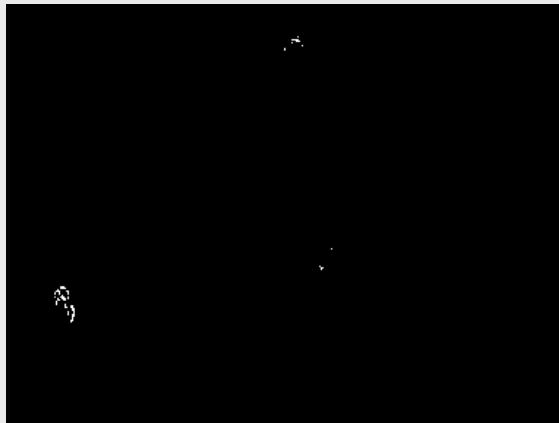
the frame



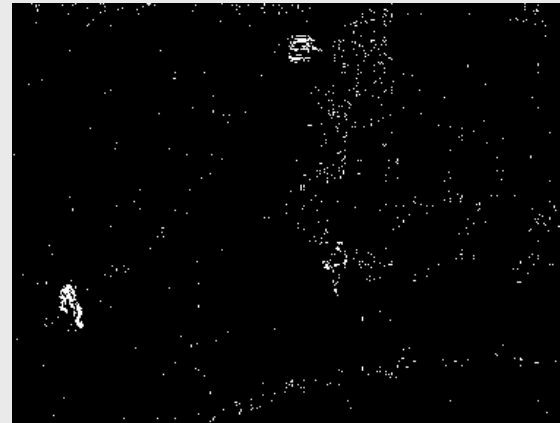
absolute  
difference



threshold:  
too high



threshold:  
too low



# The basic methods (3)

- Background as the ***average*** or the ***median*** (Velastin, 2000; Cucchiara, 2003) of the previous  $n$  frames:
  - rather fast, but very memory consuming: the memory requirement is  $n * \text{size}(\text{frame})$
- Background as the ***running average***:

$$B_{i+1} = \alpha * F_i + (1 - \alpha) * B_i$$

- $\alpha$ , the *learning rate*, is typically 0.05
- no more memory requirements

# The basic methods – rationale

- The background model at each pixel location **is based on the pixel's recent history**
- In many works, such history is:
  - just the previous  $n$  frames
  - a weighted average where recent frames have higher weight
- In essence, the background model is computed as a chronological average from the pixel's history
- No spatial correlation is used between different (neighbouring) pixel locations

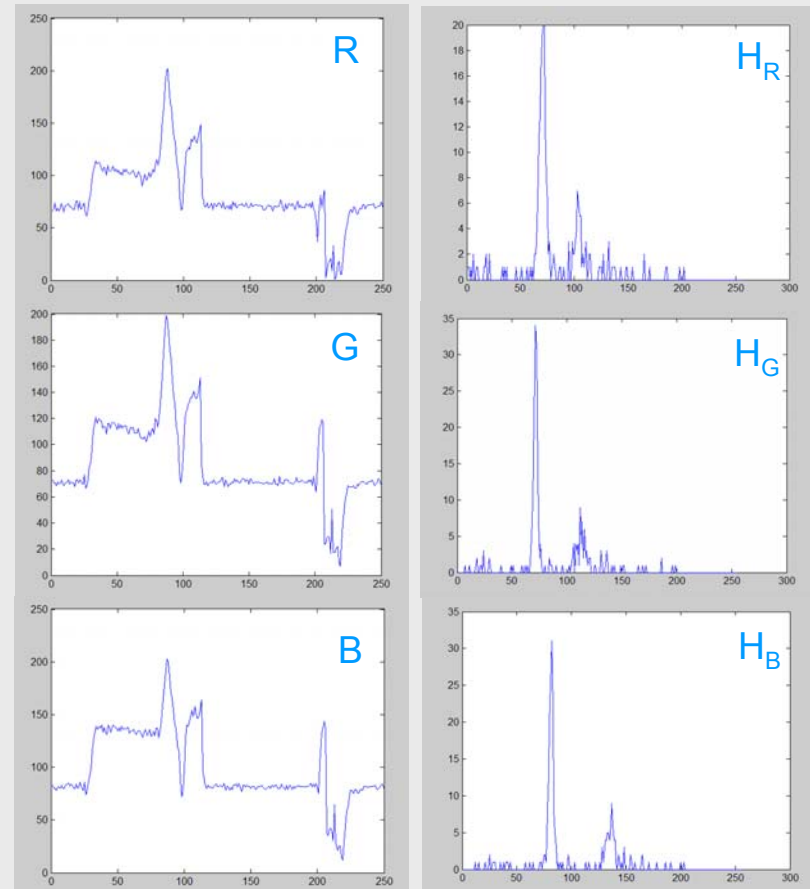


# The basic methods - histograms

- Example:



pixel  
location



sequence of  
pixel values

histograms

# The basic methods - selectivity

- At each new frame, each pixel is classified as either foreground or background
- What feedback from the classification to the background model?
  - if the pixel is classified as foreground, it is ignored in the background model
- In this way, we prevent the background model to be polluted by pixel logically not belonging to the background scene

# The basic methods – selectivity (2)

- Running average with selectivity:

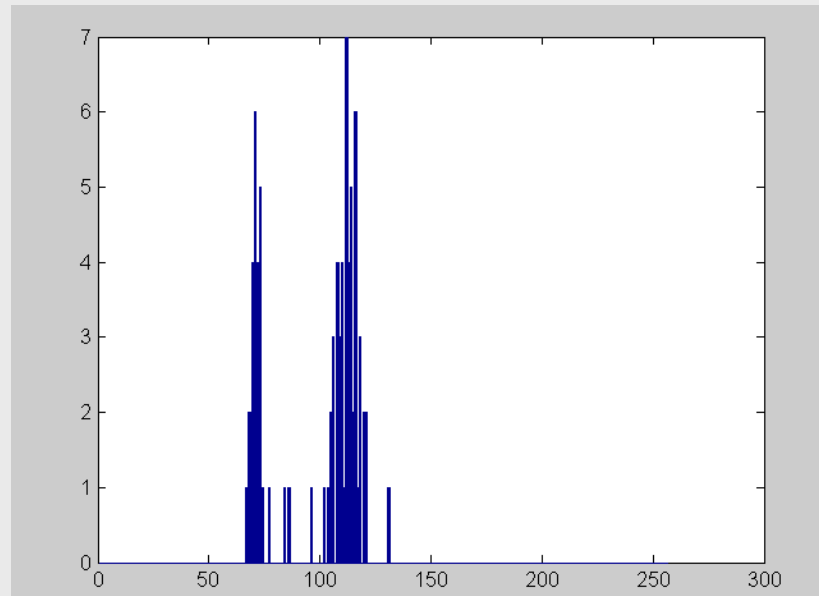
$$B_{i+1}(x, y) = \alpha F_t(x, y) + (1 - \alpha) B_t(x, y) \quad \text{if } F_t(x, y) \text{ background}$$

$$B_{i+1}(x, y) = B_t(x, y) \quad \text{if } F_t(x, y) \text{ foreground}$$

- Similarly for other methods

# The basic methods - limitations

- They do not provide an explicit method to choose the threshold
- Major: Based on a single value, they cannot cope with multiple modal background distributions; example:



# Running Gaussian average

- *Pfinder* (Wren, Azarbayejani, Darrell, Pentland, 1997):
  - fitting one Gaussian distribution  $(\mu, \sigma)$  over the histogram: this gives the background PDF
  - background PDF update: running average:

$$\mu_{t+1} = \alpha F_t + (1 - \alpha)\mu_t$$
$$\sigma_{t+1}^2 = \alpha(F_t - \mu_t)^2 + (1 - \alpha)\sigma_t^2$$

- In test  $|F - \mu| > Th$ ,  $Th$  can be chosen as  $k\sigma$
- It does not cope with multimodal backgrounds

# Mixture of Gaussians

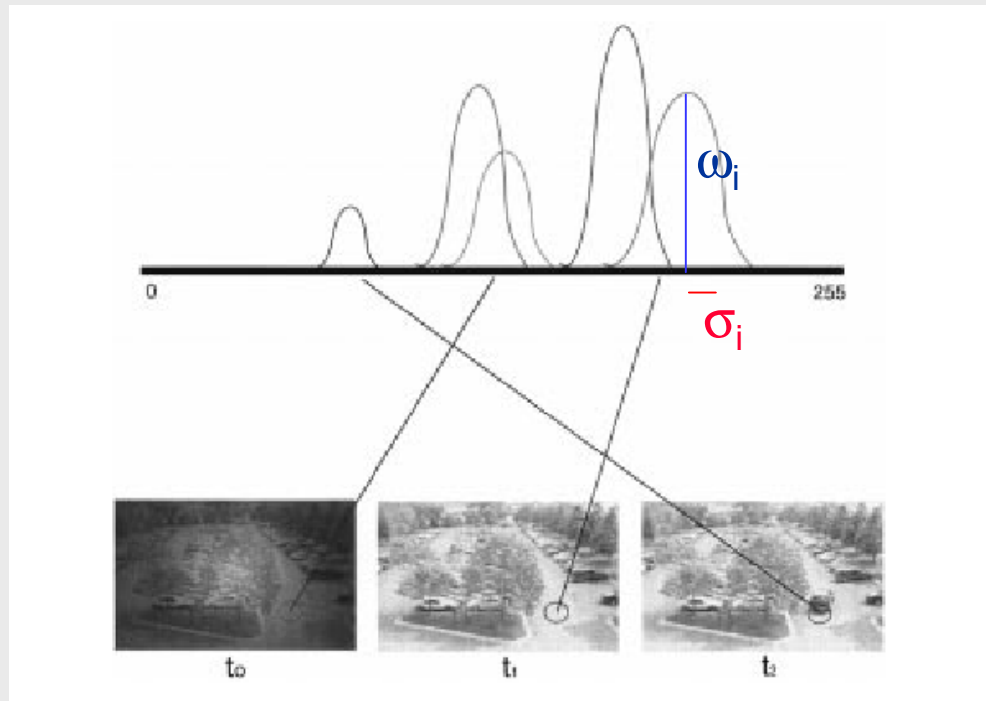
- *Mixture of K Gaussians* ( $\mu_i, \sigma_i, \omega_i$ ) (Stauffer and Grimson, 1999)
- In this way, the model copes also with multimodal background distributions; however:
  - the number of modes is arbitrarily pre-defined (usually from 3 to 5)
  - how to initialize the Gaussians?
  - how to update them over time?

# Mixture of Gaussians (2)

- All weights  $\omega_i$  are updated (updated and/or normalised) at every new frame
- At every new frame, some of the Gaussians “match” the current value (those at a distance  $< 2.5 \sigma_i$ ): for them,  $\mu_i, \sigma_i$  are updated by the running average
- The mixture of Gaussians actually models both the foreground and the background: how to pick only the distributions modeling the background?:
  - all distributions are ranked according to their  $\omega_i / \sigma_i$  and the first ones chosen as “background”

# Mixture of Gaussians (3)

- Example:



(from: I. Pavlidis, V. Morellas, P. Tsiamyrtzis, and S. Harp, "Urban surveillance systems: from the laboratory to the commercial world," *Proceedings of the IEEE*, vol. 89, no. 10, pp. 1478 -1497, 2001)



# Kernel Density Estimators

- Kernel Density Estimators (Elgammal, Harwood, Davis, 2000):
- The background PDF is given by the histogram of the  $n$  most recent pixel values, each smoothed with a Gaussian kernel (sample-point density estimator)
- If  $PDF(x) > Th$ , the  $x$  pixel is classified as background
- Selectivity
- Problems: memory requirement ( $n * size(frame)$ ), time to compute the kernel values (mitigated by a LUT approach)

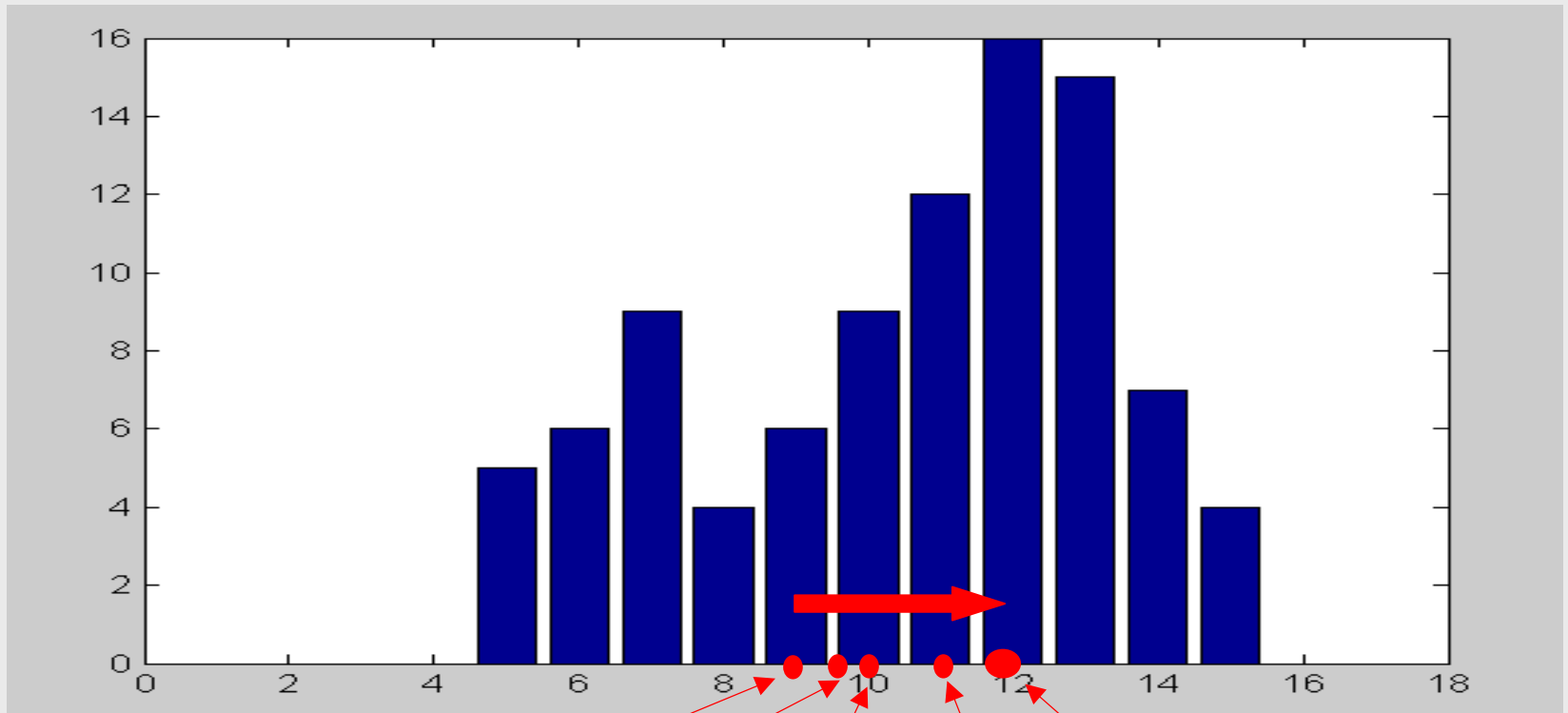
# Mean-shift based estimation

- Mean-shift based estimation (Han, Comaniciu, Davis, 2004; Piccardi, Jan, submitted 2004)
  - a gradient-ascent method able to detect the modes of a multimodal distribution together with their covariance matrix
  - iterative, the step decreases towards convergence
  - the mean shift vector:

$$m(x) = \frac{\sum_{i=1}^n x_i g((x - x_i/h)^2)}{\sum_{i=1}^n g((x - x_i/h)^2)} - x$$

# Mean-shift based estimation (2)

- Example of mean-shift trajectory in the data space:



initial position: 9    9.66    10.05    11.21    11.70: convergence

# Mean-shift based estimation (3)

- Problems:
  - a standard implementation (iterative) is way too slow
  - memory requirements:  $n * size(frame)$
- Solutions:
  - computational optimisations
  - using it only for detecting the background PDF modes at initialisation time; later, use something computationally lighter (mode propagation)

# Combined estimation and propagation

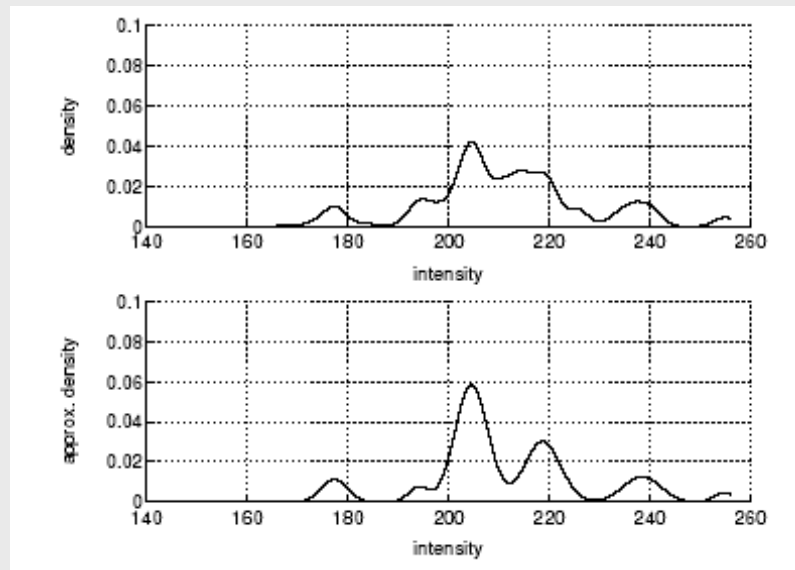
- Sequential Kernel Density Approximation (Han, Comaniciu, Davis, 2004)
  - mean-shift mode detection from samples is used only at initialisation time
  - later, modes are propagated by adapting them with the new samples:

$$PDF(x) = \alpha(new\_mode) + (1 - \alpha)(\sum existing\_modes)$$

- heuristic procedures are used for merging the existing modes (the number of modes is not fixed a priori)
- faster than KDE, low memory requirements

# Combined estimation and propagation - 2

- Example:
  - above: exact KDE
  - below: Sequential KD Approximation



*(from: B. Han, D. Comaniciu, and L.. Davis, "Sequential kernel density approximation through mode propagation: applications to background modeling," Proc. ACCV 2004)*

# Eigenbackgrounds

- Eigenbackgrounds (N. M. Oliver, B. Rosario, and A. P. Pentland, 2000)
  - Principal Component Analysis (PCA) by way of eigenvector decomposition is a way to reduce the dimensionality of a space
  - PCA can be applied to a sequence of  $n$  frames to compute the *eigenbackgrounds*
  - The authors state that it works well and is faster than a Mixture of Gaussians approach

# Eigenbackgrounds – main steps

1. The  $n$  frames are re-arranged as the columns of a matrix,  $A$
2. The covariance matrix,  $C = AA^T$ , is computed
3. From  $C$ , the diagonal matrix of its eigenvalues,  $L$ , and the eigenvector matrix,  $\Phi$ , are computed
4. Only the first  $M$  eigenvectors (eigenbackgrounds) are retained
5. Once a new image,  $I$ , is available, it is first projected in the  $M$  eigenvectors sub-space and then reconstructed as  $I'$
6. The difference  $I - I'$  is computed: since the sub-space well represents only the static parts of the scene, the outcome of this difference are the foreground objects



# Spatial correlation?

- It can be immediately evident that there exists spatial correlation between neighboring pixels. How can that be exploited?
- Low-end approach: binary morphology applied to the resulting foreground image
- Better principled: at the PDF level (for instance: Elgammal, Harwood, Davis, 2000)
- In the eigenbackground approach, the correlation matrix
- An approach formally exploiting spatial correlation: background detection based on the cooccurrence of image variations (Seki, Wada, Fujiwara, Sumi, CVPR 2003)

# Summary

Methods reviewed:

- Average, median, running average
- Mixture of Gaussians
- Kernel Density Estimators
- Mean shift (possibly optimised)
- SKDA (Sequential KD Approximation)
- Eigenbackgrounds

# Summary (2)

From the data available from the literature

- Speed
  - Fast: average, median, running average
  - Intermediate: Mixture of Gaussians, KDE, eigenbackgrounds, SKDA, optimised mean-shift
  - Slow: standard mean-shift
- Memory requirements
  - High: average, median, KDE, mean-shift
  - Intermediate: Mixture of Gaussians, eigenbackgrounds, SKDA
  - Low: running average

# Summary (3)

- Accuracy
  - Impossible to say - an unbiased comparison with a significant benchmark is needed!
  - Some methods seem to be better principled: KDE, SKDA, mean-shift
  - Mixture of Gaussians and eigenbackgrounds certainly can offer good accuracy as well
  - Simple methods such as standard average, running average, median can provide acceptable accuracy in specific applications

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